



**International
Standard**

ISO/IEC 4922-2

**Information security — Secure
multiparty computation —**

**Part 2:
Mechanisms based on secret sharing**

*Sécurité de l'information — Calcul multipartite sécurisé —
Partie 2: Mécanismes basés sur le partage de secret*

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ISO copyright office
CP 401 • Ch. de Blandonnet 8
CH-1214 Vernier, Geneva
Phone: +41 22 749 01 11
Email: copyright@iso.org
Website: www.iso.org

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Foreword

ISO (the International Organization for Standardization) and IEC (the International Electrotechnical Commission) form the specialized system for worldwide standardization. National bodies that are members of ISO or IEC participate in the development of International Standards through technical committees established by the respective organization to deal with particular fields of technical activity. ISO and IEC technical committees collaborate in fields of mutual interest. Other international organizations, governmental and non-governmental, in liaison with ISO and IEC, also take part in the work.

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A list of all parts in the ISO/IEC 4922 series can be found on the ISO website.

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Introduction

Secure multiparty computation is a cryptographic technique that computes a function on a message while maintaining the confidentiality of the message. The technique is used to outsource computations to two or more stakeholders while preserving privacy. To facilitate the effective use of secure multiparty computation and maintain interoperability, the ISO/IEC 4922 series specifies secure multiparty computation and related technologies.

Secure multiparty computation often uses cryptographic mechanisms as building blocks. For secure multiparty computation which is based on secret sharing, secret sharing schemes are used as building blocks.

Secret sharing is a cryptographic technique used to protect the confidentiality of a message by dividing it into pieces called shares. A secret sharing scheme has two main parts: a message sharing algorithm for dividing the message into shares and a message reconstruction algorithm for recovering the message from all or a subset of the shares. The ISO/IEC 19592 series specifies secret sharing and related technologies. In secure multiparty computation based on secret sharing, a message is shared among participants called parties via a message sharing algorithm. The parties compute a function on the shared message while maintaining its confidentiality and obtain shares of the function output. The function output can be obtained using a message reconstruction algorithm taking as input all or a subset of the output shares. This document specifies secure multiparty computation based on secret sharing, especially mechanisms to compute a function on the shared secret.

Information security — Secure multiparty computation —

Part 2: Mechanisms based on secret sharing

1 Scope

This document specifies the processes for secure multiparty computation mechanisms based on the secret sharing techniques which are specified in ISO/IEC 19592-2. Secure multiparty computation based on secret sharing can be used for confidential data processing. Examples of possible applications include collaborative data analytics or machine learning where data are kept secret, secure auctions where each bidding price is hidden, and performing cryptographic operations where the secrecy of the private keys is maintained.

This document specifies the mechanisms including but not limited to addition, subtraction, multiplication by a constant, shared random number generation, and multiplication with their parameters and properties. This document describes how to perform a secure function evaluation using these mechanisms and secret sharing techniques.

2 Normative references

The following documents are referred to in the text in such a way that some or all of their content constitutes requirements of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO/IEC 4922-1, *Information security — Secure multiparty computation — Part 1: General*

ISO/IEC 19592-1, *Information technology — Security techniques — Secret sharing — Part 1: General*

ISO/IEC 19592-2:2017, *Information technology — Security techniques — Secret sharing — Part 2: Fundamental mechanisms*